

# Chapter 20

## Electric Potential and Electric potential Energy

### Outline

- 20-1 Electric Potential Energy and the Electric Potential
- 20-2 Energy Conversation
- 20-3 The Electric Potential of Point Charges
- 20-4 Equipotential Surfaces and the Electric Field.
- 20-5 Capacitor and Dielectric
- 20-6 Electric Energy Storage

## 20-3 The electric potential of point charge

### Deriving electric potential of point source

Consider a point charge,  $+q$ , at the origin of the coordinate system shown in the figure. Suppose a positive test charge,  $+q_0$  is held rest at point A, a distance  $r_a$  from the origin.

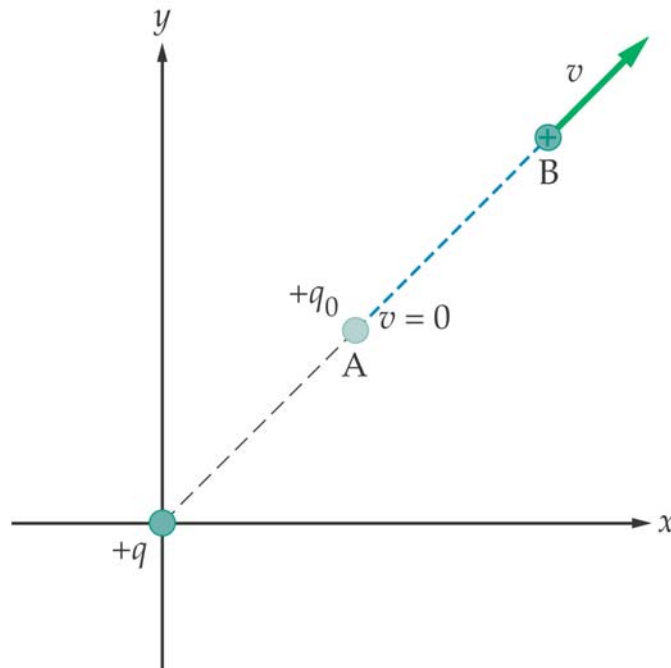


Figure 20-4. Energy Conservation in an Electrical System

After  $q_0$  moves to point B, it can be derived by integral, that the difference in electric potential energy between points A and B is

$$U_A - U_B = \frac{kq_0q}{r_A} - \frac{kq_0q}{r_B}$$

The corresponding change in electric potential is

$$V_A - V_B = U_A / q_0 - U_B / q_0 = \frac{kq}{r_A} - \frac{kq}{r_B}$$

If the test charge is moved to infinite,  $r_B \rightarrow \infty$ , we have

$$V_A - V_B = \frac{kq}{r_A}$$

We define the potential to be zero at infinite from the given charge, and we have

$$V_B = 0.$$

## Electric potential for a point charge

$$V = \frac{kq}{r} \quad (20-7)$$

SI unit: Volt, V

**Two Charges:** Electric potential energy for point charge  $q$  and  $q_0$  with  $r$  separated distance

$$U = q_0 V = \frac{kq_0 q}{r} \quad (20-8)$$

SI unit: Joule, J

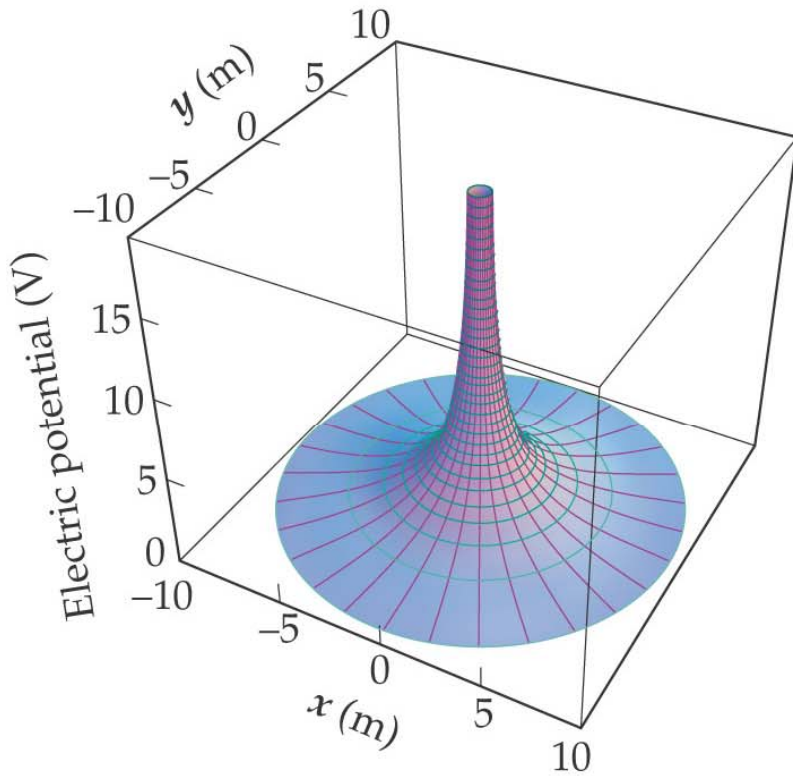
**Note:** The electric potential / energy is zero at infinite distance. **Negative charge has a minus V.**

## 20-23 The potential of a Point charge

The hydrogen atom consists of one electron and one proton. The electron orbits the proton in a circular orbit of radius  $0.529 \times 10^{-10}$  m. (a) What is the electric potential due to the proton at the electron's orbit? (b) What is the potential energy of the atom at the orbit?

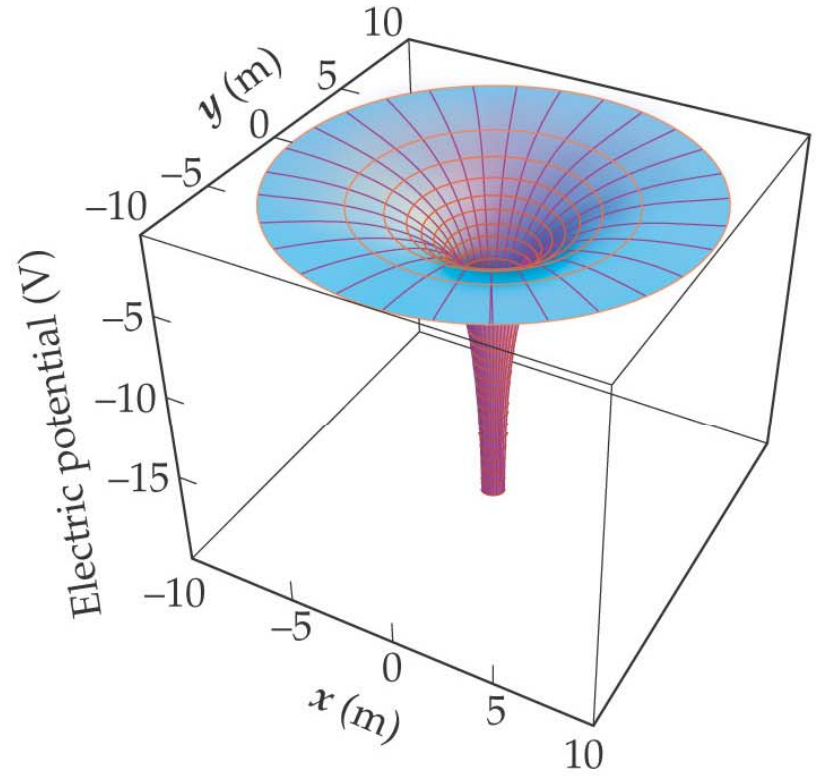
# Figure 20-5

## The Electric Potential of a Point Charge



(a)

Positive charge at origin



(b)

Negative charge at origin

## Superposition

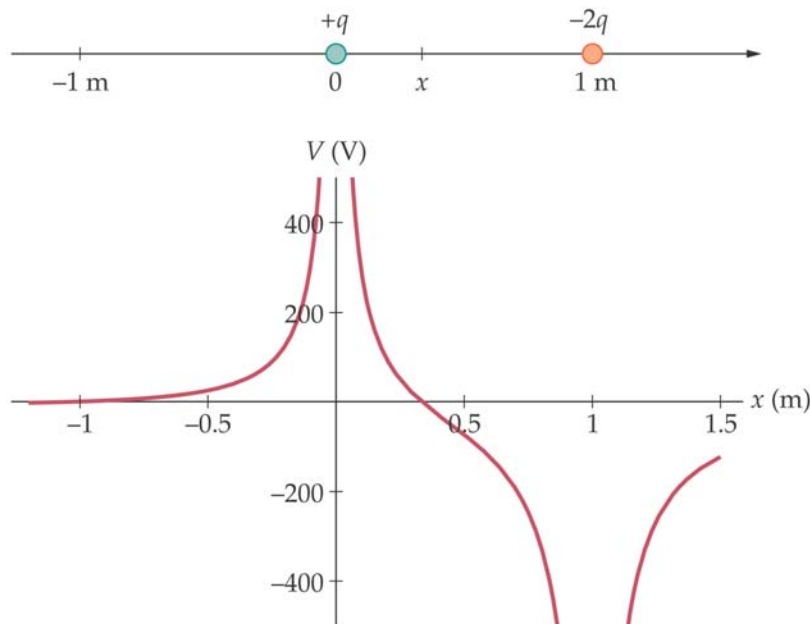
The total electric potential due to two or more charges is equal to the algebraic sum of the potentials due to each charges.

The potential of positive and negative charges may be cancelled each other. **Pay attention to the sign of the charge!**

### Example 20-3 Two point charges

A charge  $q=4.11 \times 10^{-9}$  C is placed at the origin, and a second charge of  $-2q$  is located on the  $x$  axis at the location  $x=1.00$  m.

(a) Find the electric potential **midway** between the two charges. (b) The electric potential vanish at **some** distance between the two charges. Find the this value of  $x$ .

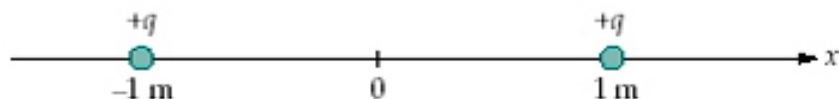


**Picture the problem**  
**Example 20-3**  
**Two Point Charges**



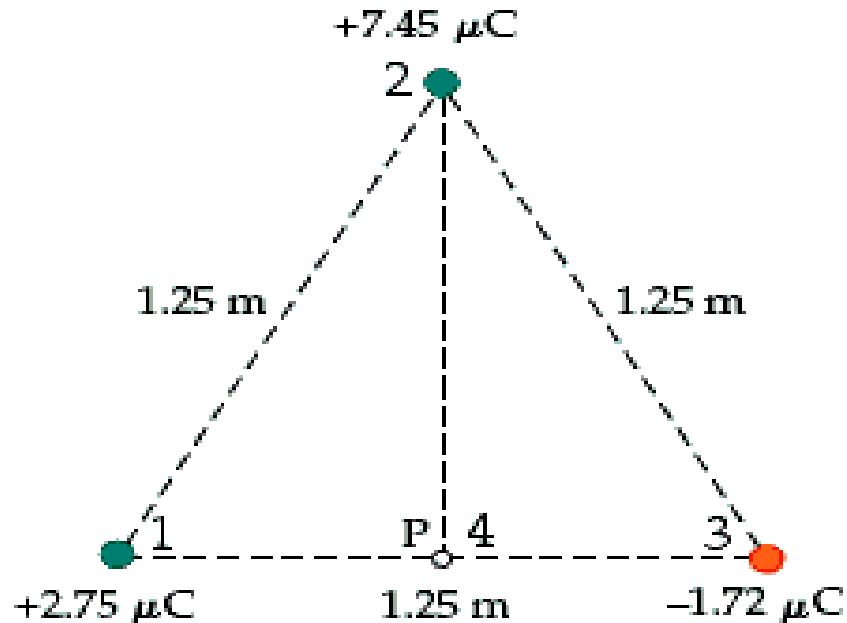
### CONCEPTUAL CHECKPOINT 20-3

Two point charges, each equal to  $+q$ , are placed on the  $x$  axis at  $x = -1$  m and  $x = +1$  m. As one moves along the  $x$  axis, does the potential look like a peak or a valley near the origin?



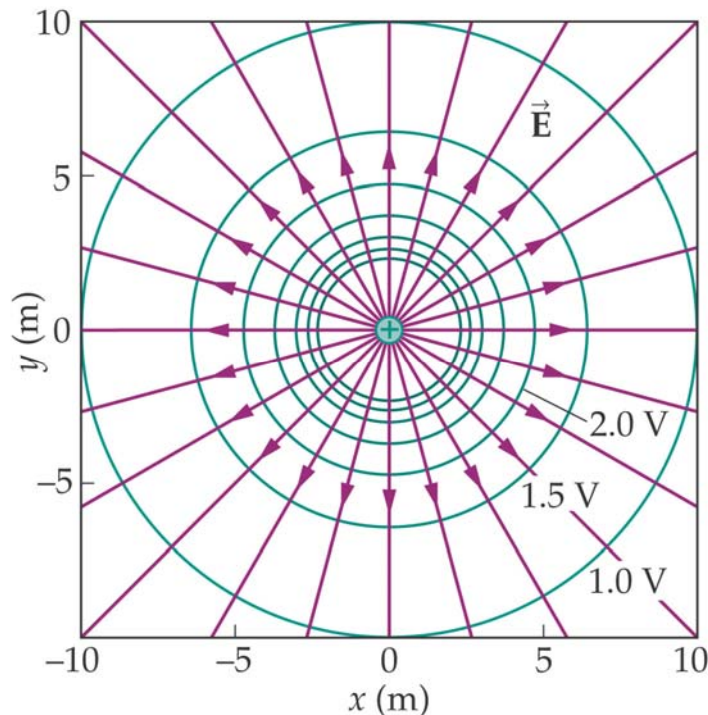
## 20-33 Multiple Charges

(a) Find the electric potential at point P in the following figure. (b) A fourth charge, with charge of  $+6.11 \text{ uC}$  and a mass  $4.71 \text{ g}$ , is released from rest at point P. What is the speed of the fourth charge when it has moved to infinite distance?



## 20-4 Equipotential surfaces and the electric field

Like the geometric contour map that is used to indicate the different altitudes, a equipotential plot/map, which consists of equipotential surface, could be used to indicate the difference of the potential.



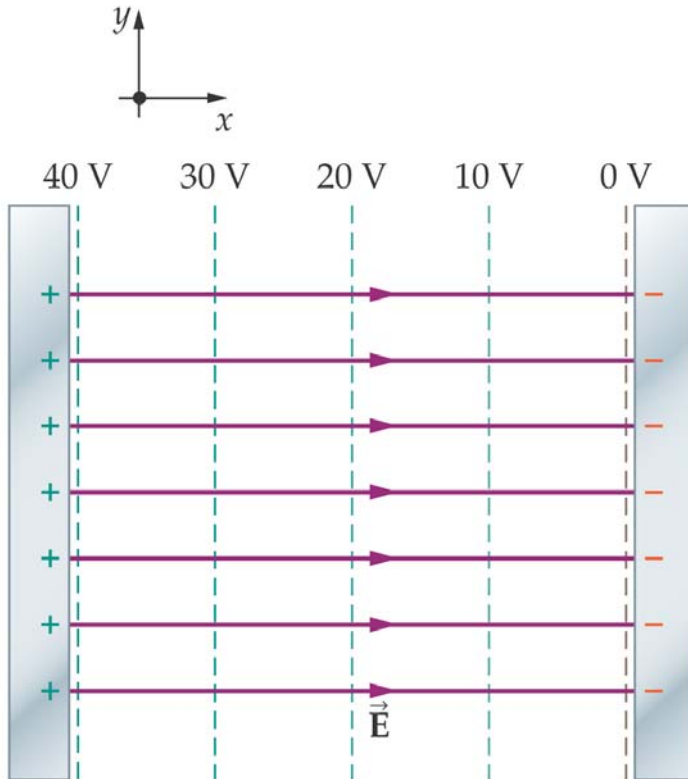
**Figure 20-6**  
**Equipotentials for a Point Charge**

## An equipotential plot must contain the following information

- 1) Relative magnitude and direction of the electric field.
  - The  $E = - \Delta V / \Delta S$ , depend on the rate of the change of the potential.
  - The electric field points in the direction of decreasing electric potential.
- 2) The electric field is always perpendicular to the equipotential surface.

# Figure 20-7

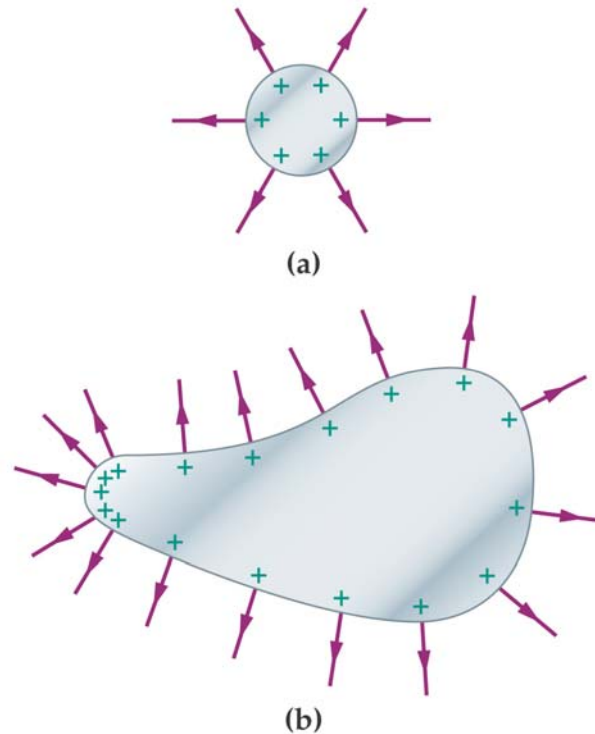
## Equipotential Surfaces for a Uniform Electrical Field



The electric field is perpendicular to the equipotentials and points in the direction of decreasing potential.

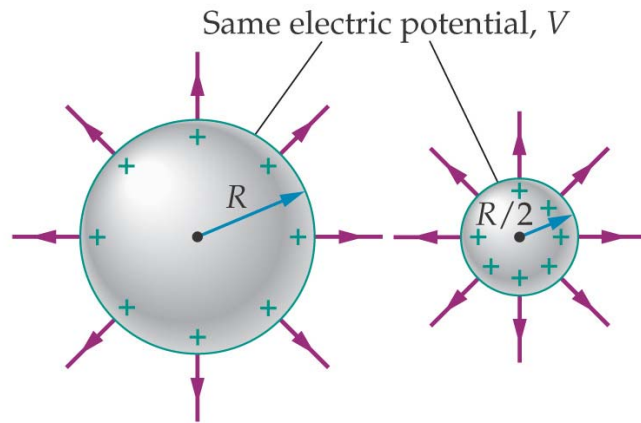
# Ideal Conductors

Charges on ideal conductor can move freely and with no work being done.

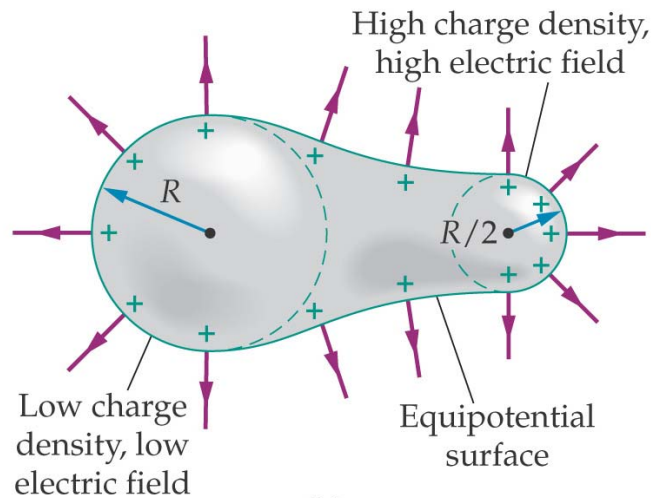


**Figure 20-9**  
**Electric Charges on the Surface of Ideal**  
**Conductors**

Why the charges have high density (large electric field) at the sharp end?



(a)



(b)

**Figure 20-10**  
**Charge Concentration Near**  
**Points**

In figure (a), the potential at its surface is the same as for a point charge  $Q$  at the center of the sphere,

$$V = \frac{kQ}{R} = \frac{k\sigma(4\pi R^2)}{R} = 4\pi k\sigma R$$

Where  $\sigma$  is the charge density.

Consider (b) with a sphere of  $R/2$ , for the same potential with (a), we have

$$V = 4\pi k\sigma_b(R/2) = 4\pi k\sigma R$$

$$\sigma_b = 2\sigma$$

This prove that small radius surface has large charge density.



# Summary

## 20-5 The Electric Potential of Point Charges

Electric potential for a point charge

$$V = \frac{kq}{r_A}$$

## 20-4 Equipotential Surfaces and the Electric Field.

- 1) Equipotential surfaces and its relationship with the electric field
- 2) For ideal conductor, charges have high density (large electric field) at the sharp end.

## Addition Information for homework

The number of signification figures after *multiplication* or *division* is equal to the number of the signification figures in the *least* accurately known quantity.

For examples:

$$21.2 / 8.5 = 2.5$$

$$2.51 / 12.23 = 30.7$$

$$17 / 2.51 = 6.8$$

$2.1 \times 10^{-2}$  is two signification figures.

### Exercise 20-2

Find the electric potential produced by a point charge of  $6.80 \times 10^{-7} \text{ C}$  at a distance of 2.60 m.

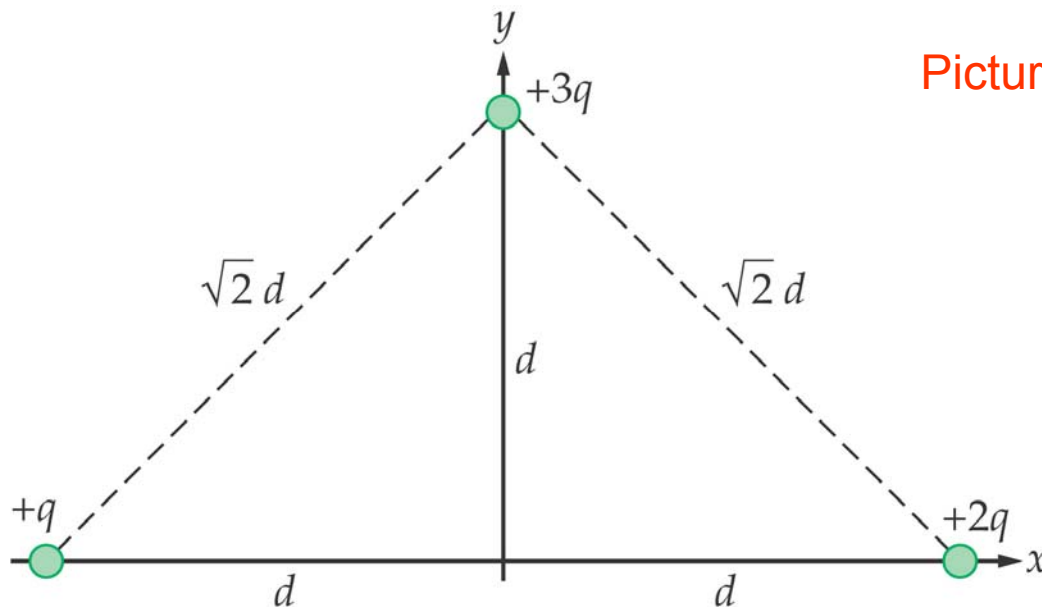
Solution:

$$\begin{aligned} V &= \frac{kq}{r} = \frac{(8.99 \times 10^9 \text{ N}\cdot\text{m}^2)(6.80 \times 10^{-7} \text{ C})}{2.60 \text{ m}} \\ &= 2350 \text{ V} \\ &= 2.35 \times 10^3 \text{ V} \end{aligned}$$

### Example 20-4 Fly Away

Two charges,  $+q$  and  $+2q$ , are held on the  $x$  axis at the location  $x=-d$  and  $x=+d$ , respectively. A third charge  $+3q$  is released from rest on the  $y$  axis at  $y=d$ .

(a) Find the electric potential due to the first two charges at the initial location of the third charge. (b) Find the initial electric potential energy of the third charge. (c) What is the kinetic energy of the third charge when it has moved infinitely far away from the other two charges?



Picture the problem

**Example 20-4  
Fly Away**

## Solution

### Part (a)

The electric potential at the initial position of the third charge is

$$V_i = \frac{k(+q)}{\sqrt{2d}} + \frac{k(+2q)}{\sqrt{2d}} = \frac{3kq}{\sqrt{2d}}$$

### Part (b)

Multiply  $V_i$  by  $(3q)$  to find the  $U$ :

$$U_i = (+3q)V_i = (+3q)\frac{3kq}{\sqrt{2d}} = \frac{9kq^2}{\sqrt{2d}}$$

### Part (c)

Since energy conservation:

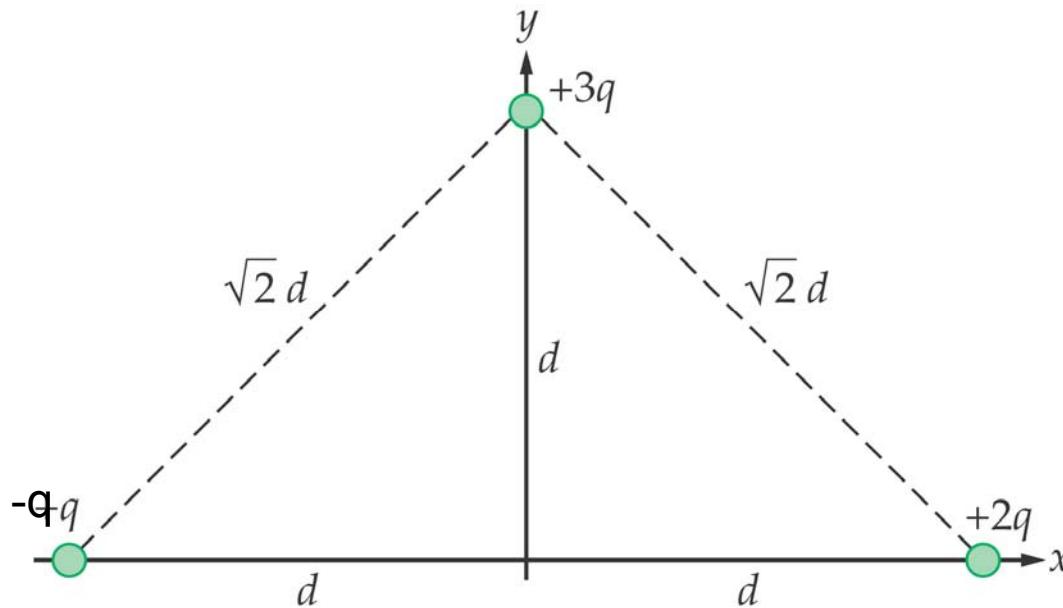
$$U_i + K_i = U_f + K_f$$

$$\frac{9kq^2}{\sqrt{2d}} + 0 = 0 + K_f$$

$$K_f = \frac{9kq^2}{\sqrt{2d}}$$

### Example 20-4 Find the electric potential energy

A system consists of three charges  $-q$  at  $(-d,0)$ ,  $+2q$  at  $(d,0)$  and  $+3q$  at  $(0,d)$ . What is total electric potential energy of the system?



Picture the problem

## Solution

1) The electric potential energy between  $-q$  and  $+2q$

$$U_{12} = \frac{k(-q)(2q)}{2d}$$

2) The electric potential energy between  $-q$  and  $+3q$

$$U_{13} = \frac{k(-q)(3q)}{\sqrt{2}d}$$

3) The electric potential energy between  $2q$  and  $+3q$

$$U_{23} = \frac{k(2q)(3q)}{\sqrt{2}d}$$

4) The total electric potential energy of the system

$$U = U_{12} + U_{13} + U_{23} = \frac{k3q^2}{\sqrt{2}d} - \frac{kq^2}{d}$$